

# DirFis: A hybrid silicon and PPAC detector array for direct reaction and fission coincidence measurements\*

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To further investigate heavy-ion reaction mechanisms and the fission of actinide nuclei using the surrogate reaction method, a compact and efficient hybrid detector array for coincidence measurements of beam-like particles and fission fragments has been developed and tested online. This detector array consists of four silicon strip detector telescopes and two parallel-plate avalanche counters. For the near-barrier  ${}^7\text{Li} + {}^{238}\text{U}$  reaction, the fission fragments correlated with the beam-like  ${}^6\text{He}$  particles originating from the transfer reaction were confirmed by analyzing the folding angle. The fission barrier height for the short-lived actinide nucleus  ${}^{239}\text{Np}$ , produced in the  $1p$  stripping channel, was extracted from its fission probability. The deduced value is in good agreement with the existing literature data.

Keywords: Hybrid detector array; Coincidence measurement; Transfer-induced fission; Fission barrier height; Fission fragment folding angle

## I. INTRODUCTION

Nuclear reactions with heavy-ions at energies around the Coulomb barrier are of great significance for studying the interplay between nuclear structure and reaction dynamics. Weakly bound nucleus induced reactions, owing to their low separation energy thresholds [1] and cluster structures [2–4], exhibit complicated reaction mechanisms of breakup, incomplete fusion and cluster transfers in the near-barrier energy region. Over the past three decades, to thoroughly investigate the reaction mechanisms induced by weakly bound nuclei, many silicon strip detector arrays have been developed worldwide, such as MUST [5], LEDA [6], EXPADES [7], GLORIA [8], MITA [9] and STARE [10]. These detector arrays have greatly advanced the experimental research in this field.

However, several key issues in weakly bound nuclear systems still remain. Among them, the competition between breakup-incomplete fusion and transfer reactions, as well as the controversy over their relative contributions, has persisted for decades [11–16]. From an experimental perspective, since both breakup and transfer processes can produce the same beam-like particles (BLP), it is difficult to effectively distinguish between these two reaction mechanisms from an inclusive measurement. To address this, various experimental techniques have been developed over the years, including  $\alpha$  decay measurements of target-like particles (TLP) [13, 15, 17], coincidence of BLP- $\gamma$  [12, 16, 18–25], and BLP-fission fragment (FF) [26–28]. Compared to the coincidence measurements with  $\alpha$ -decay or  $\gamma$ , which suffer

from the half-life restriction or uncertainty in  $\gamma$ -decay branching ratio, the coincidence with FF has the advantage of covering a wide excitation energy range and yielding more reliable quantitative results [26, 28].

In addition to reaction mechanisms, fission-related studies are also of considerable interest. Nuclear fission, since its discovery about 90 years ago, remains one of the most challenging subjects in nuclear physics both experimentally [29–31] and theoretically [29, 32, 33]. Fission is also widely utilized in power reactors, which currently generate approximately 11% of the world's electricity [34]. It also holds significant application value in interdisciplinary fields such as nuclear astrophysics, nuclear medicine and environment [35]. The fission barrier height, introduced by Bohr and Wheeler [36], is one of the most fundamental quantities describing nuclear fission. To date, information on fission barriers in actinide nuclei has been mainly obtained through direct neutron induced fission and indirect transfer surrogate methods, including  $(t, d)$  [37],  $(d, p)$  [38–40],  $(t, p)$  [41, 42],  $({}^3\text{He}, d)$  [41–43] and  $({}^{18}\text{O}, x)$  [44] reactions. Compared to neutron-induced reactions, transfer-induced fission offers a significant advantage of studying short-lived unstable nuclides, wherein the natural decay not only makes sample handling difficult but also generates intense background signals in measurements, posing substantial challenges for neutron-induced reaction studies.

To further investigate reaction mechanisms and fission related physics, a compact hybrid setup, named DirFis, consisting of silicon strip detectors and parallel-plate avalanche counters (PPACs) has been built and tested. The importance of  ${}^{239}\text{Np}$  fission, which is a key intermediate nuclide in the nuclear fuel cycle and has accumulated extensive experimental data on its fission barrier [42–44], makes it a suitable candidate for validating the reliability of the present detector array.

In this work, coincidence measurements between fission fragments and beam-like particles were performed for the weakly bound  ${}^7\text{Li} + {}^{238}\text{U}$  system at the near-barrier energy  $E_{\text{Lab}} = 36.8$  MeV. The variation of the fission probability

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69 of the target-like nucleus  $^{239}\text{Np}$  with excitation energy was  
 70 determined from the emitting BLP  $^6\text{He}$  originating from  $1p$   
 71 stripping, and the fission barrier height of  $^{239}\text{Np}$  was ex-  
 72 tracted. The design of the hybrid detector array is described in  
 73 Section II. Section III presents the offline test results. Section  
 74 IV discusses the in beam test results followed by the summary  
 75 in Section V.

## 76 II. THE HYBRID DETECTOR ARRAY

77 The detector array is illustrated in Fig. 1, where the arrow  
 78 indicates the beam direction. Four  $\Delta E$ - $E$  silicon strip de-  
 79 tector telescopes  $\text{Si}_{0-3}$  were placed at backward angles of  
 80  $112^\circ$  and  $155^\circ$  relative to the beam direction to identify the  
 81 beam-like particles. Each telescope consists of three layers  
 82 of  $50 \times 50 \text{ mm}^2$  silicon detectors: the first layer is a single-  
 83 sided silicon strip detector (SSSD) with a nominal thickness  
 84 of  $20 \mu\text{m}$ , the second layer is an SSSD with a thickness of  
 85  $300 \mu\text{m}$ , and the third layer is a quadrant silicon detector  
 86 (QSD) with a thickness of  $1000 \mu\text{m}$ . Each SSSD is segmented  
 87 into 16 strips with the strip orientations of the first two layers  
 88 perpendicular to each other, forming 256 pixels with areas of  
 89  $3.0 \times 3.0 \text{ mm}^2$ . All the SSSDs and QSDs were manufactured  
 90 by the Micron Semiconductor Ltd [45]. The first and second  
 91 layers are used to detect heavier particles such as Li and He  
 92 isotopes, while the second and third layers are used to detect  
 93 lighter particles like  $p$ ,  $d$  and  $t$ .

94 The distances from the target to the detectors are  $162.7 \text{ mm}$   
 95 for  $\text{Si}_{0,1}$  and  $167.5 \text{ mm}$  for  $\text{Si}_{2,3}$ , with an angular coverage of  
 96  $\pm 0.55^\circ$  per pixel. The total solid angle covered by the four  
 97 silicon strip detector telescopes is  $0.1\pi$ . A  $0.5 \mu\text{m}$  thick Mylar  
 98 film was installed in front of each silicon telescope to mini-  
 99 mize the influence of low-energy electrons on the first layer  
 100 silicon detectors during online experiments. All silicon de-  
 101 tectors were coupled with self-made integrated charge-sensitive  
 102 preamplifiers [46] in vacuum, working in a cooled condition  
 103 to optimize the energy resolution and ensure performance sta-  
 104 bility. These preamplifiers have been applied in several exper-  
 105 iments and exhibit excellent and stable performance [10, 47-  
 106 50].

107 Two PPACs, each with an active area of  $296 \times 200 \text{ mm}^2$ ,  
 108 were employed to detect the fission fragments. Both the en-  
 109 trance and exit windows are  $2.0\text{-}\mu\text{m}$ -thick Mylar film. Both  
 110 PPACs adopt a conventional three-electrode structure, con-  
 111 sisting of an  $X$  anode, a cathode, and a  $Y$  anode. The distance  
 112 from the anode plane to the cathode plane is  $3.0 \text{ mm}$ . The  
 113 anode wires are  $20\text{-}\mu\text{m}$ -diameter gold-plated tungsten wires  
 114 with a spacing of  $1.0 \text{ mm}$  between every two wires and cou-  
 115 pled to delay lines. Two adjacent wires in the  $X$  direction  
 116 were read out together as one channel, while three adjacent  
 117 wires in the  $Y$  direction were read out together as one. There-  
 118 fore, each PPAC has 146 position information in  $X$  direction  
 119 and 66 position information in  $Y$  direction. More detailed  
 120 description of the PPAC can be found in [51]. The electron-  
 121 ics system was used to acquire TDC time signals and ADC  
 122 energy signals. To maximize the detection efficiency with  
 123 appropriate counting rates, the two PPACs were positioned

124 at  $57^\circ$  and  $96^\circ$  respectively, based on the folding angle dis-  
 125 tribution. The forward-angle PPAC detector ( $\text{PPAC}_F$ ) was  
 126 placed at a distance of  $187 \text{ mm}$  from the target center, while  
 127 the backward-angle one ( $\text{PPAC}_B$ ) was placed at a distance of  
 128  $152 \text{ mm}$ . The covered polar angle  $\theta$  ranges from  $20.2^\circ$  to  
 129  $96.2^\circ$  and from  $52.5^\circ$  to  $140.2^\circ$ , respectively. The total solid  
 130 angle covered by the two PPAC detectors ( $\Omega_{\text{PPAC}}$ ) amounts  
 131 to  $0.85\pi$ .

132 Four PIN silicon detectors were placed at fixed forward  
 133 angles of  $\pm 15^\circ$  and  $\pm 20^\circ$  relative to the beam direction as  
 134 monitors. They were used to monitor the beam direction and  
 135 spot size, as well as to normalize reaction cross sections via  
 136 Rutherford scattering.

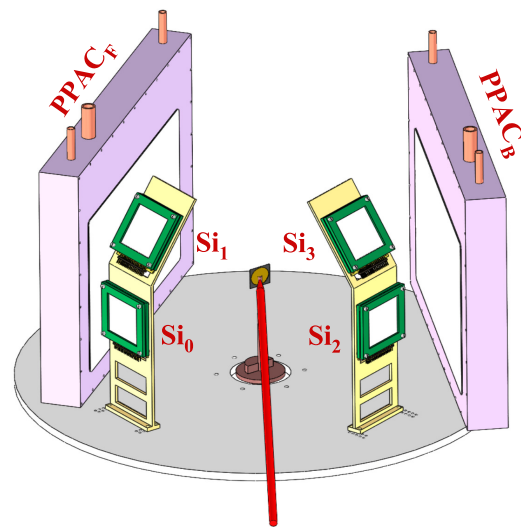


Fig. 1. (Color online) Schematic view of the hybrid detector array, mainly consisting of four  $\Delta E$ - $E$  silicon strip detector telescopes and two PPAC detectors. The long arrow indicates the beam direction.

## 137 III. OFFLINE TESTS

138 Good energy and position resolutions are essential for kine-  
 139 matic measurements, which are crucial for characterizing the  
 140 reaction processes of weakly-bound nuclei. Therefore, offline  
 141 performance tests were conducted using a three-component  $\alpha$   
 142 source for the silicon detectors and a  $^{252}\text{Cf}$  fission source for  
 143 the PPAC detectors, in order to obtain their performance and  
 144 determine the optimal operating conditions.

### 145 A. Silicon detector performance with a three-component $\alpha$ 146 source

147 The three-component  $\alpha$  source consists of  $^{239}\text{Pu}$ ,  $^{241}\text{Am}$   
 148 and  $^{244}\text{Cm}$ . The  $20\text{-}\mu\text{m}$  thick silicon layer is too thin for com-  
 149 plete energy deposition of these  $\alpha$ s, and the  $\alpha$  particles will  
 150 hit the  $300\text{-}\mu\text{m}$  layer. A typical  $E_1$ - $E_2$  energy spectrum of  $\alpha$

151 particles detected in a pixel of  $\text{Si}_0$  is shown in Fig. 2(a). The  
 152 large variation in the energy loss observed in the first silicon  
 153 layer is mainly attributed to the thickness non-uniformity of  
 154 the thin silicon detector. The total energy  $E_1+E_2$  spectrum  
 155 is shown in Fig. 2(b). The three separate groups correspond  
 156 to the three components. A Gaussian fit to the peak of 5.486  
 157 MeV  $\alpha$  particles emitted from  $^{241}\text{Am}$  yields an energy resolu-  
 158 tion of  $\sim 1.2\%$  for the total energy  $E_1+E_2$ , as shown by the  
 159 solid line.

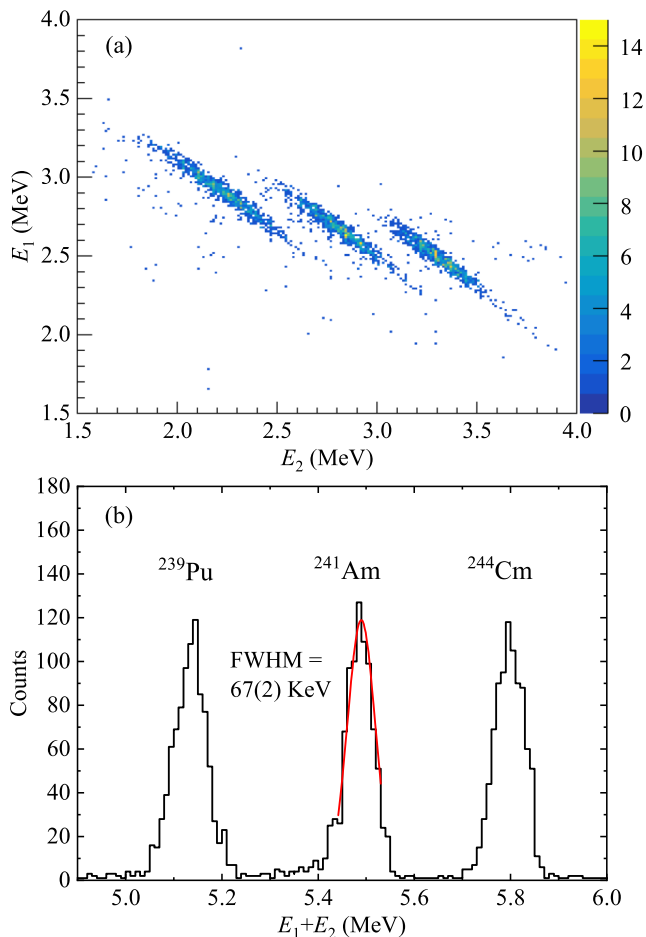


Fig. 2. (Color online) Performance of the first two layers of  $\text{Si}_0$  detector telescope tested with a three-component  $\alpha$  source. (a)  $E_1-E_2$  spectrum of the  $\alpha$  particles from the decay of the three-component  $\alpha$  source. (b) Total energy  $E_1+E_2$  spectrum. The Gaussian fitting (solid line) for the middle group gives an energy resolution of  $\sim 1.2\%$  for the 5.486 MeV  $\alpha$  peak.

#### B. PPAC position resolution with a $^{252}\text{Cf}$ source

161 The position resolution of the PPAC detector mainly depends on  
 162 the nature of the incident ions, the working gas, and the applied  
 163 high voltage. Isobutane gas with a purity of 99.99% was used  
 164 as the working gas of PPAC detectors. The optimal operating  
 165 conditions were achieved at a pressure

166 of 4.5 Torr and a high voltage of  $-550$  V for both PPACs.  
 167 A typical result obtained for  $^{252}\text{Cf}$  fission fragments under  
 168 these conditions is shown in Fig. 3. Panels (a) and (b) show  
 169 the typical position resolution spectra of  $\text{PPAC}_B$  in the  $X$   
 170 and  $Y$  directions, respectively. The position calibration was  
 171 obtained from the linear proportional relationship between the  
 172 time signal difference and the geometric position. From the  
 173 Gaussian fits to the position peaks, the average FWHM of the  
 174 detector in the  $X$  and  $Y$  direction are  $0.94 \pm 0.03$  mm and  
 175  $2.21 \pm 0.08$  mm, respectively. It can be seen that good  
 176 position resolution was achieved from both the  $X$  and  $Y$  directions.

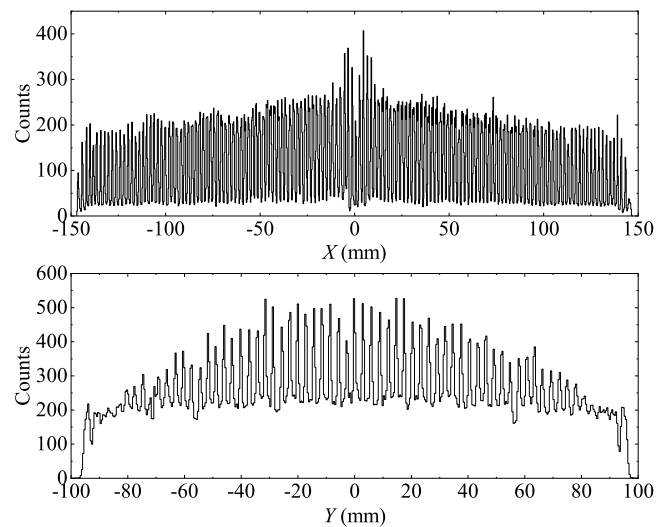


Fig. 3. Performance of the  $\text{PPAC}_B$  detector tested with a  $^{252}\text{Cf}$  source. (a) Position spectrum in the  $X$  direction. (b) Position spectrum in the  $Y$  direction.

#### IV. IN BEAM TEST

178 The experiment was conducted at the HI-13 tandem accel-  
 179 erator of the China Institute of Atomic Energy. The  $^{238}\text{U}$   
 180 target was selected considering the high fissionability of its target-  
 181 like particles after transfer reactions. The  $^{238}\text{U}$  target with a  
 182 thickness of  $370 \mu\text{g}/\text{cm}^2$  was sandwiched between a 33 nm  
 183 aluminum foil and a  $50 \mu\text{g}/\text{cm}^2$  carbon backing. The target  
 184 was fixed at the center of the hybrid detector array with a  
 185 normal angle of  $30^\circ$  relative to the beam direction, in order to  
 186 minimize the energy loss of fission fragments in the target and  
 187 the dead area caused by the target frame. The reaction energy  
 188 for  $^7\text{Li} + ^{238}\text{U}$  is  $E_{\text{lab}} = 36.8$  MeV. The irradiation time was  
 189 20 hours with a beam intensity of  $\sim 10$  nA. The low-energy  
 190  $^{79}\text{Br} + ^{238}\text{U}$  elastic scattering was selected to calibrate the  
 191 geometrical alignment of the two PPACs.

192 **A. Calibration of the PPACs by using  $^{79}\text{Br} + ^{238}\text{U}$  elastic**  
 193 **scattering**

194 Elastic scattering of  $^{79}\text{Br} + ^{238}\text{U}$  at a beam energy 170  
 195 MeV was used to calibrate the geometry of the two PPACs.  
 196 The obtained folding angle distribution of the  $^{79}\text{Br} + ^{238}\text{U}$   
 197 elastic scattering is shown in Fig. 4. The red solid line represents  
 198 the scattered beam component, while the green dashed  
 199 line represents the recoiled target nucleus component. The  
 200 good agreement of the experimental data with the kinematic  
 201 calculations confirms the good position calibration and instal-  
 202 lation geometry.

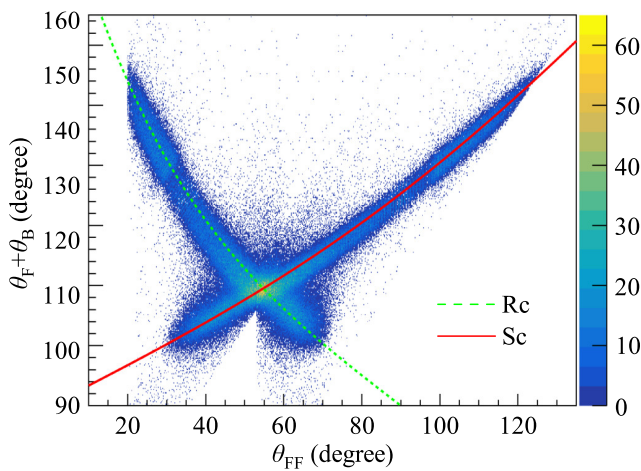


Fig. 4. (Color online) The folding angle distribution for the  $^{79}\text{Br} + ^{238}\text{U}$  elastic scattering at 170 MeV. The  $X$ -axis shows the  $\theta$  coverage angle of the PPACs, and the  $Y$ -axis shows the folding angle of the two simultaneously emitted fragments. The lines represent kinematic calculations, where the red solid line corresponds to the scattered beam component (Sc), and the green dashed line corresponds to the recoiled target nucleus component (Rc).

203 **B. Identification of beam-like particles**

204 A typical inclusive  $\Delta E$ - $E$  particle identification spectrum  
 205 measured by the silicon strip detector telescope  $\text{Si}_0$  in  $^7\text{Li} +$   
 206  $^{238}\text{U}$  at  $E_{\text{lab}} = 36.8$  MeV and  $\theta_{\text{lab}} = 155^\circ$  is shown in Fig. 5.  
 207 In Fig. 5(a),  $E_1$  is the energy loss in the first layer, and  $E_1 + E_2$   
 208 is the sum of the energy loss in the first layer and the residual  
 209 energy deposited in the second layer. He and Li isotopes  
 210 are well identified in this spectrum. The band correspond-  
 211 ing to  $^4\text{He}$  is prominent, and these particles are completely  
 212 stopped in the second layer. Specifically, the observation of  
 213  $^6\text{He}$  indicates the occurrence of the  $1p$ -stripping process in  
 214 the  $^7\text{Li}$ -induced reaction. In Fig. 5(b),  $E_2$  is the energy loss  
 215 in the second layer, and  $E_3$  is the residual energy deposited in  
 216 the third layer. In this spectrum, the hydrogen isotopes  $p$ ,  $d$ ,  
 217 and  $t$  are well identified. The  $d$  and  $t$  particles are completely  
 218 stopped in the third layer.

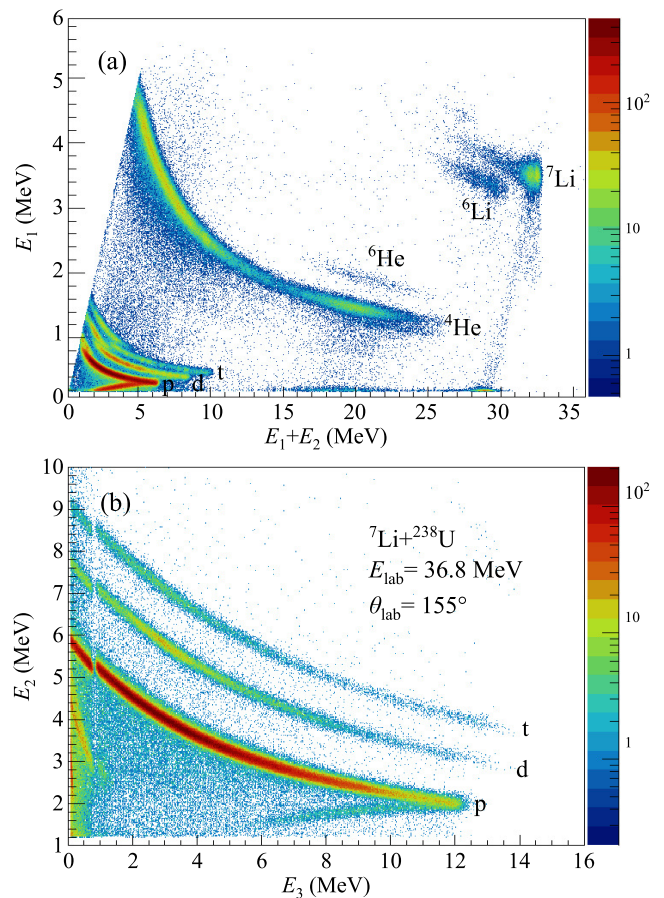


Fig. 5. (Color online) Typical particle identification spectra for light charged particles in  $^7\text{Li} + ^{238}\text{U}$  at  $E_{\text{lab}} = 36.8$  MeV and  $\theta_{\text{lab}} = 155^\circ$ . (a) Identification of the heavier particles using the first and second layers. (b) Identification of the lighter particles using the second and third layers.

219 **C.  $^6\text{He}$ -gated fission fragment folding angle distribution**

220 The  $^6\text{He}$  exit channel in the  $^7\text{Li} + ^{238}\text{U}$  system was firstly  
 221 selected to test the performance of the detector array consid-  
 222 ering its following advantages: 1) For measurement, the en-  
 223 ergy loss of scattered  $^7\text{Li}$  particles in PPAC is small, which  
 224 reduces the counting rate of PPAC especially in the angular  
 225 region with small  $\theta$  relative to the beam direction and hence  
 226 reduces the dead time for data acquisition. 2) For the emitting  
 227 channel, the origin of  $^6\text{He}$  from  $1p$  stripping should be domi-  
 228 nant compared to the breakup mechanism due to the large  
 229 proton separation energy of 9.97 MeV for  $^7\text{Li}$ . 3) For  $^6\text{He}$ ,  
 230 it has no bound excitation states, thus avoiding the ambiguity  
 231 associated with excitation energy partition in the exit channel.

232 Figure 6 shows a typical correlated energy spectrum of two  
 233 complementary fission fragments obtained from the cathodes  
 234 of the two PPACs in  $^7\text{Li} + ^{238}\text{U}$  at  $E_{\text{lab}} = 36.8$  MeV, where  
 235  $E_{\text{F}}$  and  $E_{\text{B}}$  correspond to the energy signals obtained from  
 236 PPAC<sub>F</sub> and PPAC<sub>B</sub>, respectively. It can be observed that the  
 237 heavy fragments produced in the reaction are mainly concen-  
 238 trated in the channel range of 1000-3000. Consequently, the

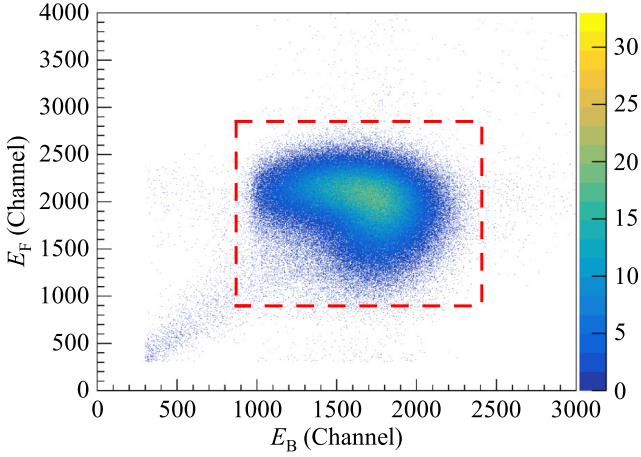


Fig. 6. (Color online) A typical correlated energy spectrum of two complementary fission fragments measured by PPAC<sub>F</sub> and PPAC<sub>B</sub> in  ${}^7\text{Li} + {}^{238}\text{U}$  at  $E_{\text{lab}} = 36.8$  MeV. The red dashed contour indicates the selected fission events used for further analysis.

clean fission events selected for subsequent analysis are enclosed within the red contour.

The folding angle distribution is a sensitive probe to select the non-complete momentum transfer events. The folding angle distribution for all events in which both fission fragments were detected by PPAC<sub>F</sub> and PPAC<sub>B</sub> in  ${}^7\text{Li} + {}^{238}\text{U}$  at  $E_{\text{lab}} = 36.8$  MeV is shown in Fig. 7 as solid circles. These events correspond to the total fission (TF) yield, including both complete-fusion fission and fission following direct reactions. It shows an obvious deviation from a Gaussian shape. A double-Gaussian fitting, shown as the solid line, was used to roughly fit the shape. The main component concentrating at  $\sim 173^\circ$  agrees with the Viola systematics [52] assuming fission from the complete fusion (CF) with full-momentum transfer. In addition, a pronounced lower angle component centered at  $\sim 168^\circ$  is observed, corresponding to the non-complete fusion events.

A total of 1790 triple coincidence events of  ${}^6\text{He}$  particles with both fission fragments detected by PPAC<sub>F</sub> and PPAC<sub>B</sub> were obtained, yielding the folding angle distribution shown in Fig. 7 as the solid triangles. It can be seen that the peak position of the  ${}^6\text{He}$  correlated fission fragments shows obvious deviation from the peak position of  $\sim 173^\circ$ . It is roughly reproduced by the single Gaussian fitting with a smaller peak angle compared to the CF, shown as the dash-dotted line in

Fig. 7. This is reasonable for a higher recoil velocity of TLP considering that the measured  ${}^6\text{He}$  particles emitted in the backward angular region will transfer larger linear momentum to the target nucleus compared to situation in CF events.

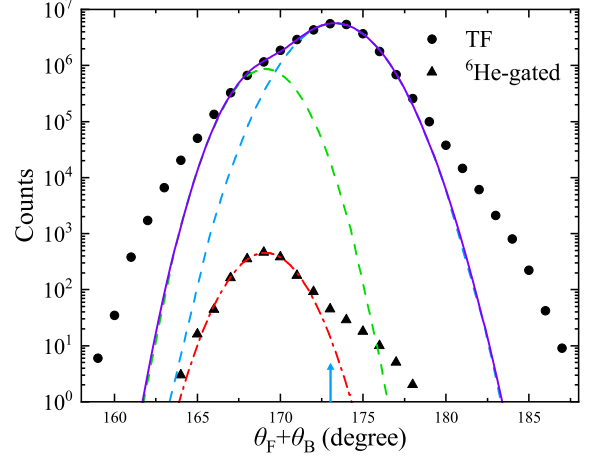


Fig. 7. (Color online) The folding angle distributions of the total fission fragments (solid circles) and  ${}^6\text{He}$ -gated fission fragments (solid triangles) obtained in  ${}^7\text{Li} + {}^{238}\text{U}$  at  $E_{\text{lab}} = 36.8$  MeV. The double-Gaussian fitting curve is for the total fission, where the higher peak corresponds the CF components in accordance with the arrow position calculated by assuming Viola kinematics [52], and the lower peak corresponds to the non-complete momentum transfer components. The solid line is the summed one. The fitting for  ${}^6\text{He}$ -coincident one is shown as the dash-dotted line.

#### D. Fission probability of ${}^{239}\text{Np}$ as a function of excitation energy obtained from the ${}^{238}\text{U}({}^7\text{Li}, {}^6\text{He}){}^{239}\text{Np}$ reaction channel

The fission barrier height corresponds to the excitation energy where the fission probability is half of the maximum of the first-chance fission probability [53]. Experimentally, the method based on the variation of the fission probability with excitation energy has been widely used to obtain the fission barrier height of a nuclide [41, 43, 44, 54].

In the present case, the measured  ${}^6\text{He}$  particles can only populate the ground state, so all the excitation energy in the exit channel is imparted to the TLP  ${}^{239}\text{Np}$ . By measuring the energy  $E_b$  and emission angle  $\theta$  of  ${}^6\text{He}$ , the excitation energy of  ${}^{239}\text{Np}$  can be unambiguously determined by applying the conservation laws of energy and momentum [54]:

$$E^* = Q_{\text{gg}} - \frac{E_a(M_a - M_B) - E_b(M_b + M_B) + 2\sqrt{M_a M_b E_{\text{lab}} E_b} \cos \theta}{M_B}, \quad (1)$$

where  $a$ ,  $b$  and  $B$  represent the beam, beam-like and target-like particles, respectively.  $M_i$  represents the mass of each nucleus involved in the reaction,  $Q_{\text{gg}}$  is the  $Q$ -value of the transfer reaction populating the ground states for the two

emitting particles.

The fission probability  $P_{\text{Fis}}$ , extracted from the double coincidence between the BLP and either FF, is defined as the ratio of the fission cross section  $\sigma_{\text{Fis}}$  to the reaction cross

section  $\sigma_r$  for forming the compound nucleus in the specific transfer channel [44, 54]. For PPAC<sub>i</sub>, the corresponding quantity  $P_{\text{Fis}}^i$  is given by

$$P_{\text{Fis}}^i(E^*) = \frac{N_{\text{BLP-FF}_i}(E^*)}{N_{\text{BLP}}(E^*)\varepsilon_i(E^*)}, \quad (2)$$

where  $N_{\text{BLP}}$  is the count of the outgoing beam-like  ${}^6\text{He}$  particles detected by the silicon strip detectors, corresponding to TLP events;  $N_{\text{BLP-FF}_i}$  is the count obtained from coincidence between BLP and any fission fragment detected by either PPAC detector, corresponding to events where the TLPs undergo fission;  $\varepsilon_i$  is the fission detection efficiency defined as [41]

$$\varepsilon_i = \frac{2\Omega_{\text{PPAC}_i}}{4\pi}, \quad (3)$$

The factor of 2 in the numerator is due to producing two fission fragments in a fission event. This is the so-called geometrical efficiency. This definition has been widely used [41, 43, 44] and confirmed reliable within a deviation of 10%-level recently for  ${}^{243}\text{Am}({}^3\text{He}, t){}^{243}\text{Cm}$  within an excitation energy range of 5.5-15.0 MeV by comparing with a Monte Carlo simulation result based on a high statistical measurement of the fission fragment angular distribution [54]. In addition, corrections for both the intrinsic efficiency and the random coincidence efficiency ( $P_{\text{Fis}}^{\text{random}}$ ) were applied. The intrinsic efficiency was determined by comparing the number of backward fission fragments identified in coincidence with the forward PPAC within a confined angular region expected to be covered by the backward PPAC, and was found to be approximately 99.6% in the present experiment.  $P_{\text{Fis}}^{\text{random}}$  was estimated from the correlation between elastically scattered  ${}^7\text{Li}$  particles and fission fragments, for which no real fission is expected, and was found to be approximately 0.01.

The experimentally extracted fission probability  $P_{\text{Fis}}$  obtained from coincidence with PPAC<sub>F</sub> as a function of excitation energy  $E^*$  for the target-like nucleus  ${}^{239}\text{Np}$  is shown in Fig. 8 as solid circles, where the error bars represent only statistical uncertainties. The measurement covers a wide excitation energy range below 12.5 MeV, and the obtained  $P_{\text{Fis}}^{\text{max}}$  is 0.57(4), averaged over all pixels of the silicon detector telescopes. The result obtained from coincidence with PPAC<sub>B</sub> is similar, giving  $P_{\text{Fis}}^{\text{max}} = 0.63(4)$ . A significant discrepancy is observed between the present ( $P_{\text{Fis}}^{\text{max}}$ ) result and the literature value reported by JAEA [44]. The lower value reported by JAEA is attributed to the strong horizontal tail of elastically scattered particles produced in the above-barrier  ${}^{18}\text{O} + {}^{237}\text{Np}$  reaction, which strongly affects the extraction of the fission probability in the excitation energy region near the fission barrier, as well as to the use of a relatively large 0.8 MeV bin width, resulting from poor energy resolution.

For the fitting to the fission barrier, it should be pointed out that due to the fact that the rising part of the fission probability curve in Fig. 8 contains only a few data points, this limited energy resolution precludes the observation of any resonance (class-II) sub-barrier structures, which are sensitive to both the inner and outer barrier heights [55]. Although actinide

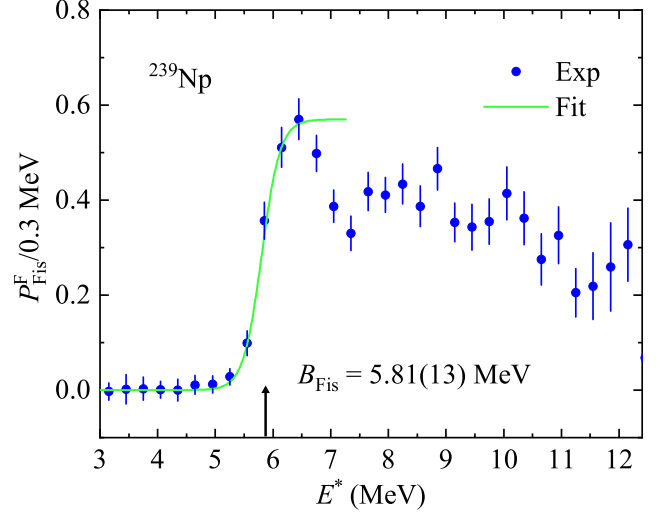


Fig. 8. (Color online) Experimentally extracted fission probability  $P_{\text{Fis}}^F$  as a function of the excitation energy  $E^*$  for  ${}^{239}\text{Np}$  by using the  ${}^{238}\text{U}({}^7\text{Li}, {}^6\text{He}){}^{239}\text{Np}$  at  $E_{\text{lab}} = 36.8$  MeV. The solid circles represent the experimental data, and the solid line is the fitting curve by using Eq. 4.

Table 1. The extracted values of  $P_{\text{Fis}}^{\text{max}}$  and  $B_{\text{Fis}}$  for  ${}^{239}\text{Np}$  from  ${}^{238}\text{U}({}^7\text{Li}, {}^6\text{He}){}^{239}\text{Np}$  reaction channel by using coincidence with PPAC<sub>F</sub> or PPAC<sub>B</sub>.

| Method              | $P_{\text{Fis}}^{\text{random}}$ | $P_{\text{Fis}}^{\text{max}}$ | $B_{\text{Fis}}$ |
|---------------------|----------------------------------|-------------------------------|------------------|
| BLP-FF <sub>F</sub> | 0.01                             | 0.57(4)                       | 5.81(13)         |
| BLP-FF <sub>B</sub> | 0.01                             | 0.63(4)                       | 5.82(12)         |

nuclei typically exhibit a complex double-humped fission barrier structure, it is well known that the use of a single-humped Hill-Wheeler approximation allows for a consistent derivation of the barrier height corresponding to the higher one determined by the double-humped fission barrier model [56]. The Hill-Wheeler fitting formula is expressed as [57]:

$$P_{\text{Fis}}(E^*) = \frac{P_{\text{Fis}}^{\text{max}}}{1 + \exp\left[\frac{2\pi(B_{\text{Fis}} - E^*)}{\hbar\omega}\right]}, \quad (4)$$

where  $P_{\text{Fis}}^{\text{max}}$ ,  $B_{\text{Fis}}$ , and  $\hbar\omega$  are adjustable parameters representing the maximum fission probability for the first-chance fission, fission barrier height, and fission barrier curvature, respectively.

Using Eq. 4, the fit was carried out over the sub-barrier and first-chance fission energy region. The fitting result, shown by the green solid curve in Fig. 8, reproduces the rising part of the fission probability curve well, and the extracted fission barrier heights  $B_{\text{Fis}}$  are listed in Table 1. As shown in the table, the extracted values of  $P_{\text{Fis}}^{\text{max}}$  and  $B_{\text{Fis}}$  are consistent for different fission fragment emission angles. This provides experimental evidence that the effect of angular anisotropy on the extracted results is minor [54].

The comparison of the average value of the extracted fission barrier height  $5.82 \pm 0.13$  MeV for  ${}^{239}\text{Np}$  from this work with the literature data [42–44] is shown in Table 2. It can be

Table 2. The extracted fission barrier heights for  $^{239}\text{Np}$  from this work in comparison with the literature data [42–44].

| Reaction   | $B_{\text{Fis}}$ (MeV) | Refs.     |
|--|------------------------|-----------|
| $^{238}\text{U}(^7\text{Li}, ^6\text{He})^{239}\text{Np}$      | $5.82 \pm 0.13$        | This work |
| $^{237}\text{Np}(^{18}\text{O}, ^{16}\text{O})^{239}\text{Np}$ | $5.86 \pm 0.09$        | [44]      |
| $^{238}\text{U}(^3\text{He}, d)^{239}\text{Np}$                | $5.85 \pm 0.30$        | [42]      |
| $^{238}\text{U}(^3\text{He}, d)^{239}\text{Np}$                | $5.70 \pm 0.20$        | [43]      |

seen that the present experimental result is in good consistency with the available data [42–44], validating the feasibility of determining fission barrier heights via transfer-induced fission using the present detector array.

## V. SUMMARY

In this work, a hybrid detector array for coincidence measurements of the direct reaction products and the fission fragments has been designed and fabricated. The combination of large-area silicon strip detectors and large-sensitive-area PPAC detectors provides a large solid-angle coverage of  $0.95\pi$  for the detector array, significantly improving the coincidence detection efficiency and hence enabling the extension to the reaction channels with smaller cross sections.

The present hybrid detector array has been applied to FF-BLP coincidence measurement for the weakly bound  $^7\text{Li} +$

$^{238}\text{U}$  system at  $E_{\text{lab}} = 36.8$  MeV. Benefiting from the good energy and angular resolutions of the silicon strip detectors for  $^6\text{He}$ , a good excitation energy resolution for the excitation energy of  $^{239}\text{Np}$  was obtained. The folding angle distribution gives further support for incomplete momentum transfer in the beam-like  $^6\text{He}$  emitting channel. Furthermore, the  $B_{\text{Fis}}$  of  $^{239}\text{Np}$  was extracted from the dependence of fission probability on excitation energy. The result is in good agreement with the available results. The reliability of extraction of the fission barrier height based on nucleon transfer reactions induced by light projectiles by using the present setup has been validated. This opens up the possibility of supplementing experimental fission data for more short-lived and highly radioactive actinide nuclides. On the other hand, the quantitative extraction of breakup- or transfer-induced fission in the  $\alpha$ - and  $t$ - emitting channels by using the obtained data is in progress.

## AUTHOR CONTRIBUTIONS

All authors contributed to the study conception and design. Material preparation was performed by C.J. Lin, H.M. Jia, J. Feng, and Y.J. Qiu. Data analysis and the first draft of the manuscript were prepared by S.X. Zhu. All authors commented on previous versions of the manuscript and approved the final version.

## REFERENCES

- [1] L.F. Canto, P.R.S. Gomes, R. Donangelo et al., Fusion and breakup of weakly bound nuclei, *Phys. Rep.* **424**, 1-111 (2006). <https://doi.org/10.1016/j.physrep.2005.10.006>
- [2] R. Kaur, B.B. Singh, M. Kaur et al., Investigating  $^6,7\text{Li}$ -induced reactions on  $^{235,238}\text{U}$  through a collective clusterization approach, *Phys. Rev. C* **108**, 034611 (2023). <https://doi.org/10.1103/PhysRevC.108.034611>
- [3] W.V. Oertzen, M. Freer, Y. Kanada-En'yo, Nuclear clusters and nuclear molecules, *Phys. Rep.* **432**, 43-113 (2006). <https://doi.org/10.1016/j.physrep.2006.07.001>
- [4] K. Wei, Y.L. Ye, Z.H. Yang, Clustering in nuclei: progress and perspectives, *Nucl. Sci. Tech.* **35**, 216 (2024). <https://doi.org/10.1007/s41365-024-01588-x>
- [5] Y. Blumenfeld, F. Auger, J.E. Sauvestre et al., MUST: A silicon strip detector array for radioactive beam experiments, *Nucl. Instr. Meth. A* **421**, 471-491 (1999). [https://doi.org/10.1016/S0168-9002\(98\)01178-4](https://doi.org/10.1016/S0168-9002(98)01178-4)
- [6] T. Davinson, W. Bradfield-Smith, S. Cherubini et al., Louvain-Edinburgh Detector Array (LEDA): a silicon detector array for use with radioactive nuclear beams, *Nucl. Instr. Meth. A* **454**, 350-358 (2000). [https://doi.org/10.1016/S0168-9002\(00\)00479-4](https://doi.org/10.1016/S0168-9002(00)00479-4)
- [7] M. Romoli, E. Vardaci, A. Anastasio et al., EXPADES: A new detector system for charged particles in experiments with RIBs, *Nucl. Instr. Meth. B* **266**, 4637-4642 (2008). <https://doi.org/10.1016/j.nimb.2008.05.121>
- [8] G. Marquinez-Durán, L. Acosta, R. Berjillos et al., GLORIA: A compact detector system for studying heavy ion reactions using radioactive beams, *Nucl. Instr. Meth. A* **755**, 69-77 (2014). <https://doi.org/10.1016/j.nima.2014.04.002>
- [9] N.R. Ma, L. Yang, C.J. Lin et al., MITA: A Multilayer Ionization-chamber Telescope Array for low-energy reactions with exotic nuclei, *Eur. Phys. J. A* **55**, 87 (2019). <https://doi.org/10.1140/epja/i2019-12765-7>
- [10] Y.S. Wu, G.L. Zhang, C.J. Lin et al., STARE: a new detector array for exploring the breakup reaction mechanisms induced by weakly bound nuclei, *Nucl. Sci. Tech.* **36**, 214 (2025). <https://doi.org/10.1007/s41365-025-01783-4>
- [11] L. Yang, C.J. Lin, H.M. Jia et al., Experimental investigations on near-barrier reactions with weakly-bound nuclei at the China Institute of Atomic Energy, *Eur. Phys. J. A* **61**: 124 (2025). <https://doi.org/10.1140/epja/s10050-025-01598-2>
- [12] V.V. Parkar, S.K. Sharma, R. Palit et al., Investigation of complete and incomplete fusion in the  $^7\text{Li} + ^{124}\text{Sn}$  reaction near Coulomb barrier energies, *Phys. Rev. C* **97**, 014607 (2018). <https://doi.org/10.1103/PhysRevC.97.014607>
- [13] M. Dasgupta, P.R.S. Gome, D.J. Hinde et al., Effect of breakup on the fusion of  $^6\text{Li}$ ,  $^7\text{Li}$ , and  $^9\text{Be}$  with heavy nuclei, *Phys. Rev. C* **70**, 024606 (2004). <https://doi.org/10.1103/PhysRevC.70.024606>
- [14] L. Jin, A.M. Moro, Unraveling the reaction mechanisms leading to partial fusion of weakly bound nuclei, *Phys. Rev. Lett.* **123**, 232501 (2019). <https://doi.org/10.1103/PhysRevLett.123.232501>

- [15] K.J. Cook, E.C. Simpson, L.T. Bezzina et al., Origins of Incomplete Fusion Products and the Suppression of Complete Fusion in Reactions of  ${}^7\text{Li}$ , *Phys. Rev. Lett.* **122**, 102501 (2019). <https://doi.org/10.1103/PhysRevLett.122.102501>
- [16] A. Shrivastava, A. Navin, A. Diaz-Torres et al., Role of the cluster structure of  ${}^7\text{Li}$  in the dynamics of fragment capture, *Phys. Lett. B* **718**, 931-936 (2013). <https://doi.org/10.1016/j.physletb.2012.11.064>
- [17] M. Dasgupta, D.J. Hinde, R.D. Butt et al., Fusion versus breakup: Observation of large fusion suppression for  ${}^9\text{Be} + {}^{208}\text{Pb}$ , *Phys. Rev. Lett.* **82**, 1395 (1999). <https://doi.org/10.1103/PhysRevLett.82.1395>
- [18] D.R. Zolnowski, H. Yamada, S.E. Cala et al., Evidence for "Massive Transfer" in Heavy-Ion Reactions on Rare-Earth Targets, *Phys. Rev. Lett.* **41**, 92 (1978). <https://doi.org/10.1103/PhysRevLett.41.92>
- [19] S. Bottoni, S. Leoni, B. Fornal et al., Cluster-transfer reactions with radioactive beams: A spectroscopic tool for neutron-rich nuclei, *Phys. Rev. C* **92**, 024322 (2015). <https://doi.org/10.1103/PhysRevC.92.024322>
- [20] S.K. Pandit, A. Shrivastava, K. Mahata et al., Unraveling the reaction mechanism for large alpha production and incomplete fusion in reactions involving weakly bound stable nuclei, *Phys. Lett. B* **820**, 136570 (2021). <https://doi.org/10.1016/j.physletb.2021.136570>
- [21] S.K. Pandit, A. Shrivastava, K. Mahata et al., Investigation of large  $\alpha$  production in reactions involving weakly bound  ${}^7\text{Li}$ , *Phys. Rev. C* **96**, 044616 (2017). <https://doi.org/10.1103/PhysRevC.96.044616>
- [22] M.K. Pradhan, A. Mukherjee, P. Basu et al., Fusion of  ${}^6\text{Li}$  with  ${}^{159}\text{Tb}$  at near-barrier energies, *Phys. Rev. C* **83**, 064606 (2011). <https://doi.org/10.1103/PhysRevC.83.064606>
- [23] R. Prajapat, M. Maiti, Probing the influence of incomplete fusion in the  ${}^6\text{Li} + {}^{89}\text{Y}$  reaction up to 7.2 MeV/nucleon energy, *Phys. Rev. C* **103**, 034620 (2021). <https://doi.org/10.1103/PhysRevC.103.034620>
- [24] P.K. Rath, S. Santra, N.L. Singh et al., Complete fusion in  ${}^7\text{Li} + {}^{144,152}\text{Sm}$  reactions, *Phys. Rev. C* **88**, 044617 (2013). <https://doi.org/10.1103/PhysRevC.88.044617>
- [25] M.L. Wang, G.X. Zhang, S.P. Hu et al., Study on the reaction channels in the  ${}^6\text{Li} + {}^{89}\text{Y}$  system with multi-angular proton and deuteron- $\gamma$  coincidence analysis, *Nucl. Phys. A* **1049**, 122914 (2024). <https://doi.org/10.1016/j.nuclphysa.2024.122914>
- [26] A. Pal, S. Santra, D. Chattopadhyay et al., Measurement of incomplete fusion cross sections in  ${}^{6,7}\text{Li} + {}^{238}\text{U}$  reactions, *Phys. Rev. C* **99**, 024620 (2019). <https://doi.org/10.1103/PhysRevC.99.024620>
- [27] R. Raabe, J.L. Sida, J.L. Charvet et al., No enhancement of fusion probability by the neutron halo of  ${}^6\text{He}$ , *Nature* **431**, 823-826 (2004). <https://doi.org/10.1038/nature02984>
- [28] R. Raabe, C. Angulo, J.L. Charvet et al., Fusion and direct reactions around the barrier for the systems  ${}^{7,9}\text{Be}$ ,  ${}^7\text{Li} + {}^{238}\text{U}$ , *Phys. Rev. C* **74**, 044606 (2006). <https://doi.org/10.1103/PhysRevC.74.044606>
- [29] K.H. Schmidt, B. Jurado, Review on the progress in nuclear fission—experimental methods and theoretical descriptions, *Rep. Prog. Phys.* **81**, 106301 (2018). <https://doi.org/10.1088/1361-6633/aacfa7>
- [30] A.N. Andreyev, K. Nishio, K.H. Schmidt, Nuclear fission: a review of experimental advances and phenomenology, *Rep. Prog. Phys.* **81**, 016301 (2018). <https://doi.org/10.1088/1361-6633/aa82eb>
- [31] A. Chatillon, J. Taïeb, H. Alvarez-Pol et al., Experimental study of nuclear fission along the thorium isotopic chain: From asymmetric to symmetric fission, *Phys. Rev. C* **99**, 054628 (2019). <https://doi.org/10.1103/PhysRevC.99.054628>
- [32] A. Bulgac, S. Jin, I. Stetcu, Nuclear fission dynamics: Past, present, needs, and future, *Front. Phys.* **8**, 63 (2020). <https://doi.org/10.3389/fphy.2020.00063>
- [33] M. Bender, R. Bernard, G. Bertsch et al., Future of nuclear fission theory, *J. Phys. G: Nucl. Part. Phys.* **47**, 113002 (2020). <https://doi.org/10.1088/1361-6471/abab4f>
- [34] M.D. Mathew, Nuclear energy: A pathway towards mitigation of global warming, *Prog. Nucl. Energy* **143**, 104080 (2022). <https://doi.org/10.1016/j.pnucene.2021.104080>
- [35] M. Eichler, A. Arcones, A. Kelic et al., The role of fission in neutron star mergers and its impact on the r-process peaks, *Astrophys. J.* **808**, 30 (2015). <https://doi.org/10.1088/0004-637X/808/1/30>
- [36] N. Bohr, J.A. Wheeler, The Mechanism of Nuclear Fission, *Phys. Rev.* **56**, 426 (1939). <https://doi.org/10.1103/PhysRev.56.426>
- [37] H.C. Britt, J.D. Cramer, Fission-Fragment Angular Correlations for  ${}^{233}\text{U}$ ,  ${}^{235}\text{U}$ , and  ${}^{239}\text{Pu}$  ( $t, df$ ) Reactions, *Phys. Rev.* **181**, 1634 (1969). <https://doi.org/10.1103/PhysRev.181.1634>
- [38] J.A. Northrop, R.H. Stokes, K. Boyer, Measurement of the Fission Thresholds of  ${}^{239}\text{Pu}$ ,  ${}^{233}\text{U}$ ,  ${}^{235}\text{U}$ , and  ${}^{238}\text{U}$  Using the ( $d, p$ ) Reaction, *Phys. Rev.* **115**, 1277 (1959). <https://doi.org/10.1103/PhysRev.115.1277>
- [39] Q. Ducasse, B. Jurado, M. Aïche et al., Investigation of the  ${}^{238}\text{U}(d, p)$  surrogate reaction via the simultaneous measurement of  $\gamma$ -decay and fission probabilities, *Phys. Rev. C* **94**, 024614 (2016). <https://doi.org/10.1103/PhysRevC.94.024614>
- [40] P. Glässel, H. Rösler, H.J. Specht, Intermediate structure in the  ${}^{239}\text{Pu}(d, pf)$  reaction, *Nucl. Phys. A* **256**, 220-242 (1976). [https://doi.org/10.1016/0375-9474\(76\)90105-6](https://doi.org/10.1016/0375-9474(76)90105-6)
- [41] B.B. Back, O. Hansen, H.C. Britt et al., Fission of doubly even actinide nuclei induced by direct reactions, *Phys. Rev. C* **9**, 1924 (1974). <https://doi.org/10.1103/PhysRevC.9.1924>
- [42] B.B. Back, H.C. Britt, O. Hansen et al., Fission of odd- $A$  and doubly odd actinide nuclei induced by direct reactions, *Phys. Rev. C* **10**, 1948 (1974). <https://doi.org/10.1103/PhysRevC.10.1948>
- [43] A. Gavron, H.C. Britt, E. Konecny et al.,  $\Gamma_n/\Gamma_f$  for actinide nuclei using ( ${}^3\text{He}, df$ ) and ( ${}^3\text{He}, tf$ ) reactions, *Phys. Rev. C* **13**, 2374 (1976). <https://doi.org/10.1103/PhysRevC.13.2374>
- [44] K.R. Kean, K. Nishio, K. Hirose et al., Validation of the multinucleon transfer method for the determination of the fission barrier height, *Phys. Rev. C* **100**, 014611 (2019). <https://doi.org/10.1103/PhysRevC.100.014611>
- [45] Micron Semiconductor Ltd., Royal Bldg, Marlborough Rd. Lancing, Sussex, UK BN15 8UN, private communication.
- [46] D.X. Wang, C.J. Lin, L. Yang et al., Compact 16-channel integrated charge-sensitive preamplifier module for silicon strip detectors, *Nucl. Sci. Tech.* **31**, 48 (2020). <https://doi.org/10.1007/s41365-020-00755-0>
- [47] H.M. Jia, C.J. Lin, B. Paes et al., No sub-Coulomb-barrier fusion enhancement due to positive  $Q$ -value two-neutron stripping: The  ${}^{18}\text{O} + {}^{58}\text{Ni}$  case, *Phys. Rev. C* **111**, 034606 (2025). <https://doi.org/10.1103/PhysRevC.111.034606>
- [48] H.R. Wang, C.J. Lin, N.R. Ma et al., The heavy-ion time-of-flight spectrometer HiToF, *Nucl. Sci. Tech.* **36**, 53 (2025). <https://doi.org/10.1007/s41365-025-01819-9>
- [49] L. Yang, C.J. Lin, H.M. Jia et al., Optical model potentials for  ${}^6\text{He} + {}^{64}\text{Zn}$  from  ${}^{63}\text{Cu}({}^7\text{Li}, {}^6\text{He}){}^{64}\text{Zn}$

- 588 reactions, Phys. Rev. C **95**, 034616 (2017).  
 589 <https://doi.org/10.1103/PhysRevC.95.034616>
- 590 [50] L. Yang, C.J. Lin, H.M. Jia et al., Is the Disper-  
 591 sion Relation Applicable for Exotic Nuclear Sys-  
 592 tems? The Abnormal Threshold Anomaly in the  ${}^6\text{He}$   
 593 +  ${}^{209}\text{Bi}$  System, Phys. Rev. Lett. **119**, 042503 (2017).  
 594 <https://doi.org/10.1103/PhysRevLett.119.042503>
- 595 [51] X.L. Wei, F.H. Guan, H.R. Yang, et al., Development of  
 596 Parallel Plate Avalanche Counter for heavy ion collision in  
 597 radioactive ion beam, Nucl. Eng. Technol. **52**, 575 (2020).  
 598 <https://doi.org/10.1016/j.net.2019.08.020>
- 599 [52] V.E. Viola, K. Kwiatkowski, M. Walker, Systematics of fission  
 600 fragment total kinetic energy release, Phys. Rev. C **31**, 1550  
 601 (1985). <https://doi.org/10.1103/PhysRevC.31.1550>
- 602 [53] R. Vandenbosch, J.R. Huizenga, *Nuclear Fission* (Academic,  
 603 New York, 1973), p. 227.
- 604 [54] G. Kessedjian, B. Jurado, G. Barreau et al., Fission  
 605 probabilities of  ${}^{242}\text{Am}$ ,  ${}^{243}\text{Cm}$ , and  ${}^{244}\text{Cm}$  induced  
 606 by transfer reactions, Phys. Rev. C **91**, 044607 (2015).  
 607 <https://doi.org/10.1103/PhysRevC.91.044607>
- 608 [55] S. Bjørnholm, J.E. Lynn, The double-humped fis-  
 609 sion barrier. Rev. Mod. Phys. **52**, 725 (1980).  
 610 <https://doi.org/10.1103/RevModPhys.52.725>
- 611 [56] J.D. Cramer, J.R. Nix, Exact Calculation of the Penetrability  
 612 Through Two-Peaked Fission Barriers, Phys. Rev. C **2**, 1048  
 613 (1970). <https://doi.org/10.1103/PhysRevC.2.1048>
- 614 [57] D.L. Hill J.A. Wheeler, Nuclear Constitution and the Inter-  
 615 pretation of Fission Phenomena, Phys. Rev. **89**, 1102 (1953).  
 616 <https://doi.org/10.1103/PhysRev.89.1102>